

# Channel Coordination

Marketing Litterature

- Centralized Control

-Non-linear Pricing

# Two supply chain examples

- Early day fish farming industry (1980s)
- Distribution of Industrial Gases

A photograph of a log train moving through a snowy forest. The logs are stacked high on a train, and the background shows snow-covered trees and a misty atmosphere. The image is slightly blurred to convey motion.

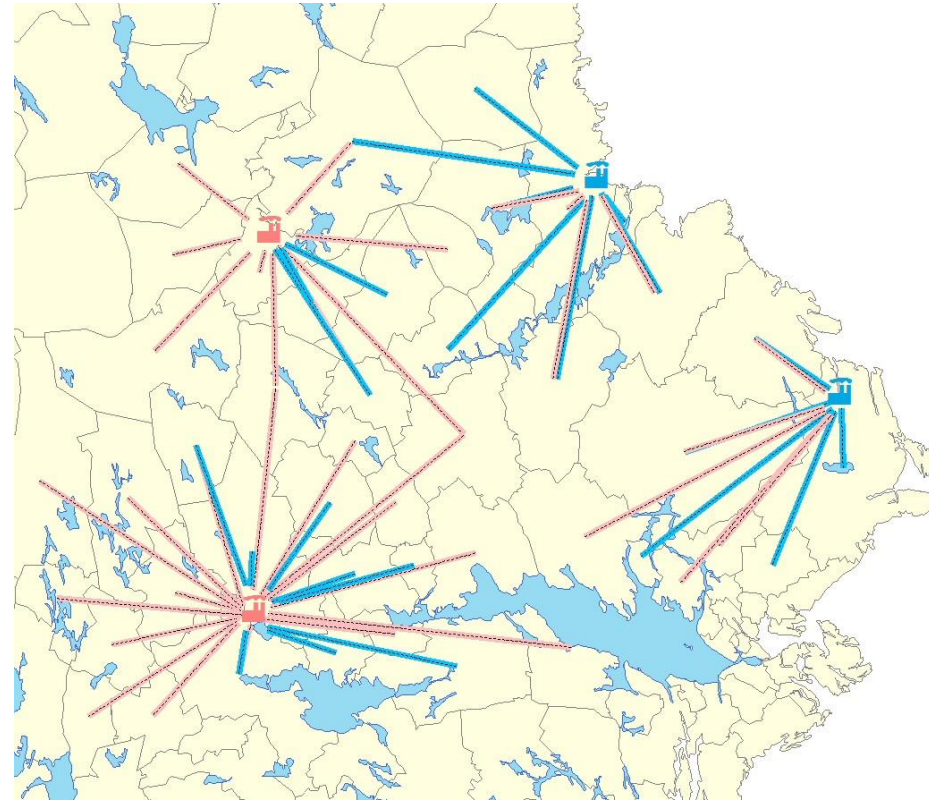
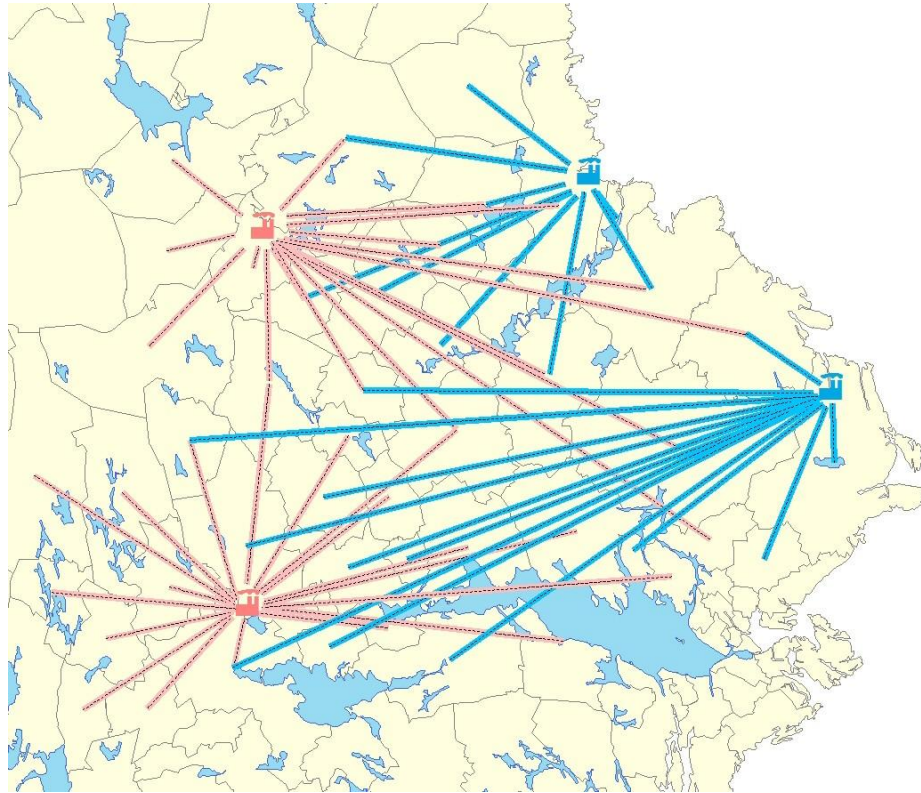
# Cost Allocation to Achieve Collaborative Transportation Solutions

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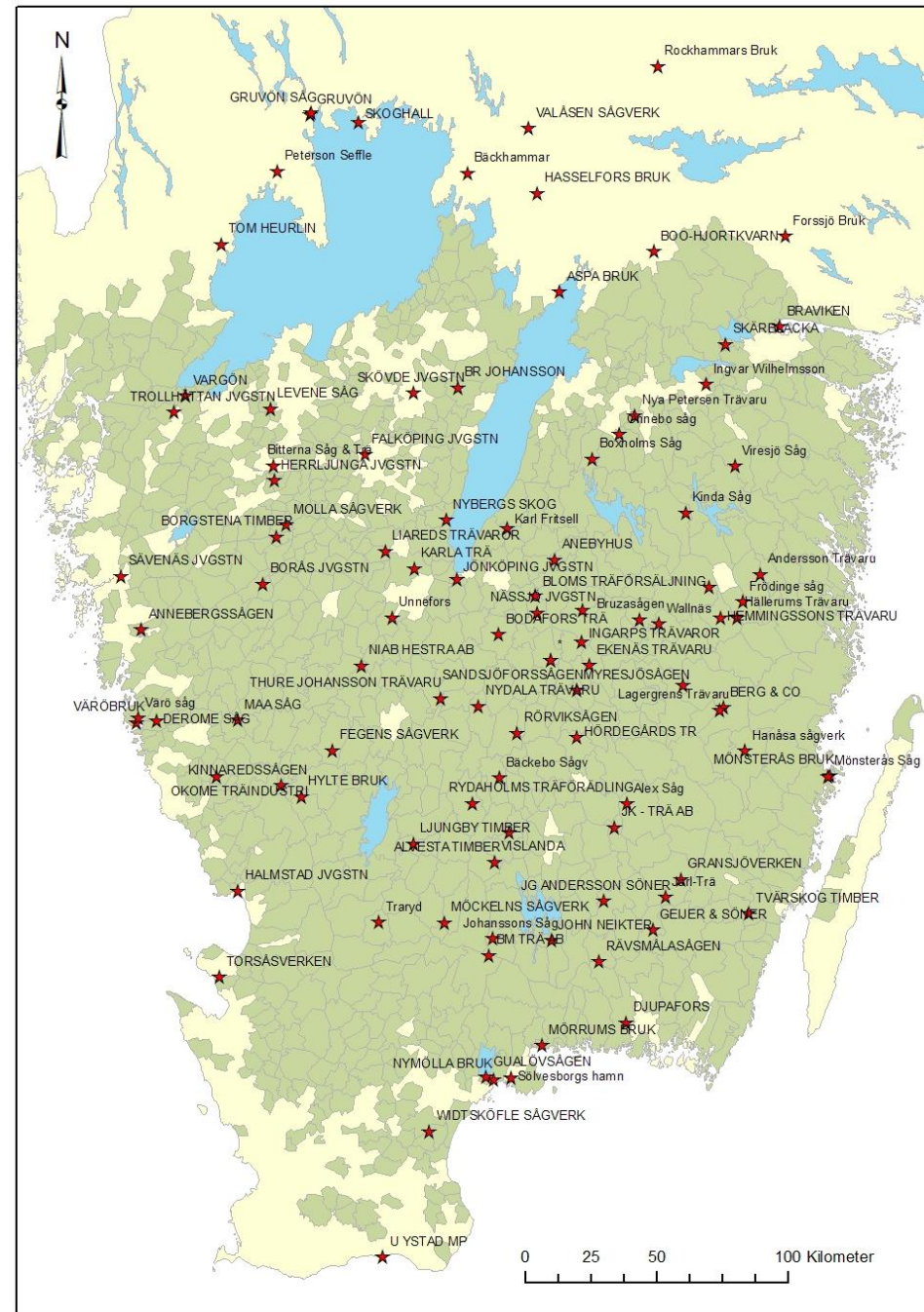
**Maud Göthe Lundgren** VTI, Sweden

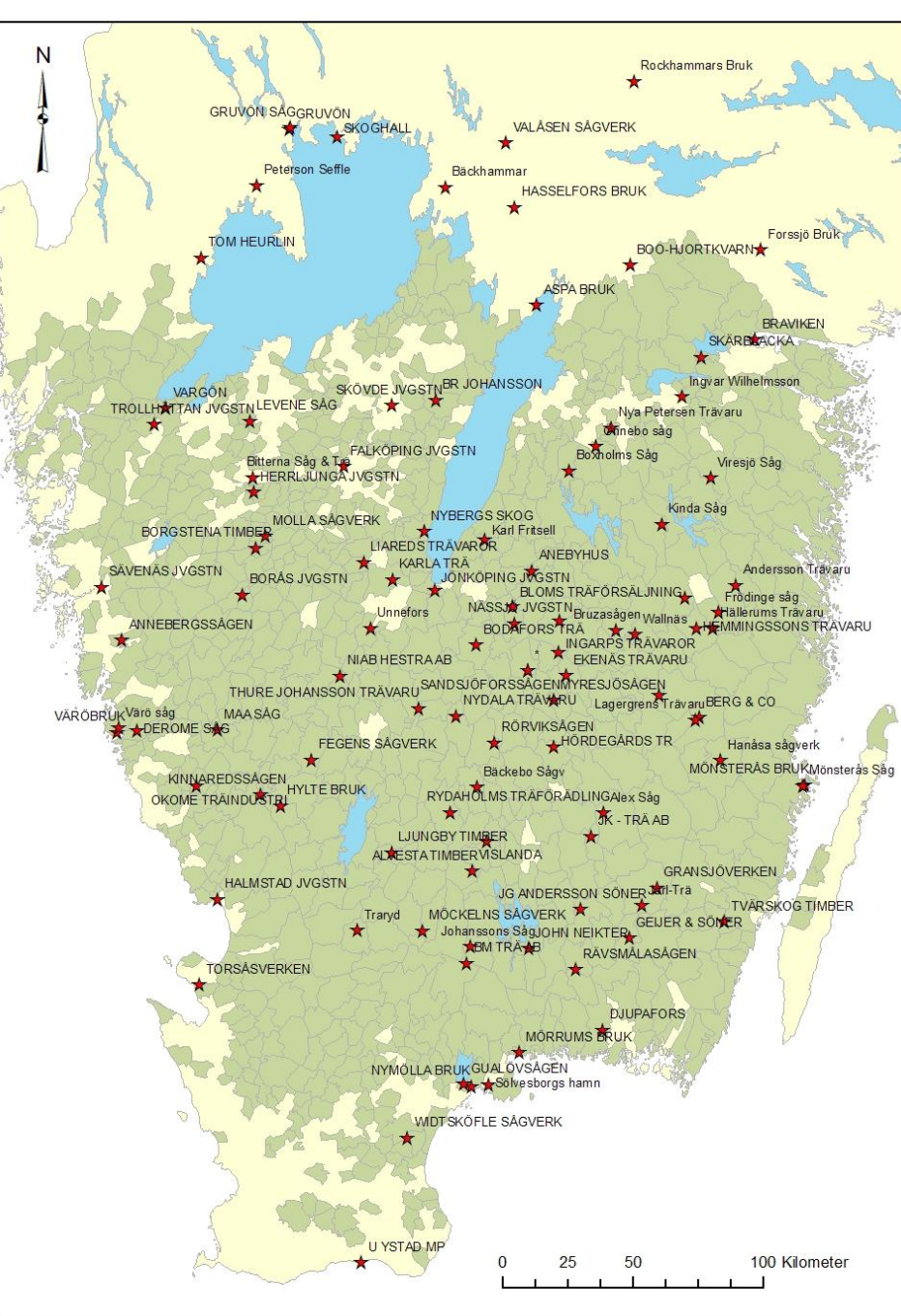
# Co-operation two companies



# Case study

- 8 participating companies in southern Sweden (monthly volumes)
- Analysis done by Skogforsk (The Forest Research Institute of Sweden)
- 898 supply points
- 101 demand points
- 39 assortments, 12 assortment groups





Company	Volume	Proportion (%)
Company 1	77,361	8,76
Company 2	301,660	34,16
Company 3	94,769	10,73
Company 4	44,509	5,04
Company 5	232,103	26,29
Company 6	89,318	10,12
Company 7	36,786	4,17
Company 8	6,446	0,73
<b>Total</b>	<b>882,952</b>	

opt1: direct flows (individual)  
opt2: backhaul flows (individual)

opt3: direct flows (collaboration)  
opt4: backhaul flows (collaboration)

Company	Real	opt 1	opt 2	opt 3	opt 4
Company 1	3,894	3,778	3,640		
Company 2	15,757	14,859	14,684		
Company 3	4,828	4,742	4,703		
Company 4	2,103	2,067	2,043		
Company 5	10,704	10,340	10,153		
Company 6	5,084	4,959	4,826		
Company 7	1,934	1,884	1,877		
Company 8	0,333	0,333	0,332		
All				39,253	38,315
Total	44,637	42,963	42,257	39,253	38,315
Saving (%)	0,00	3,75	5,33	12,06	14,16

# Optimization model

- # supply points: 4842
- # demand points: 310
- # constraints: 5,053
- # variables (direct flows): 240,000
- # variables (backhaul flows): > 100 million
- # used variables:  
240,000 + 125,000 through column generation

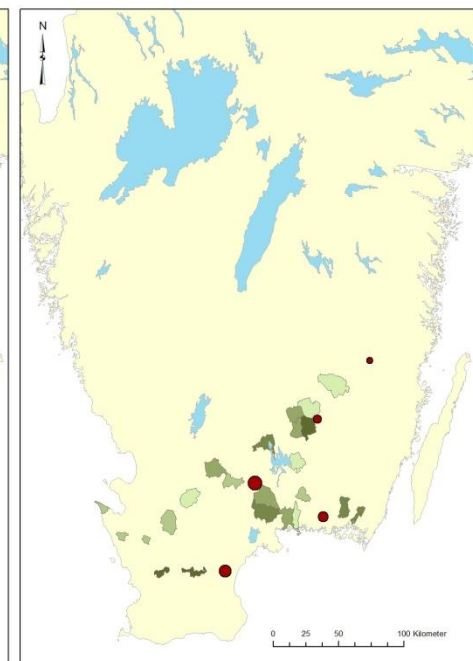
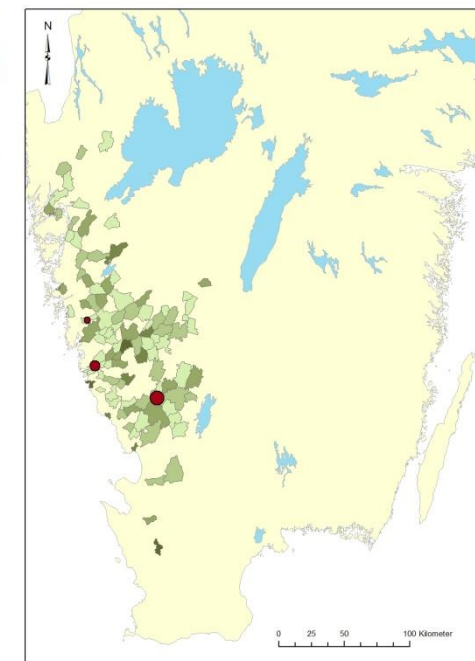
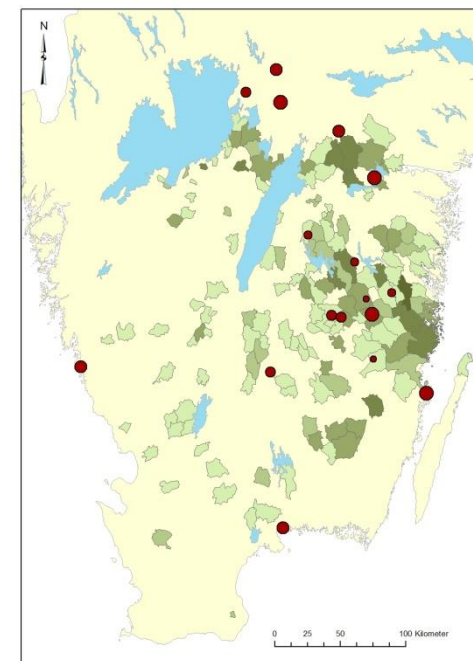
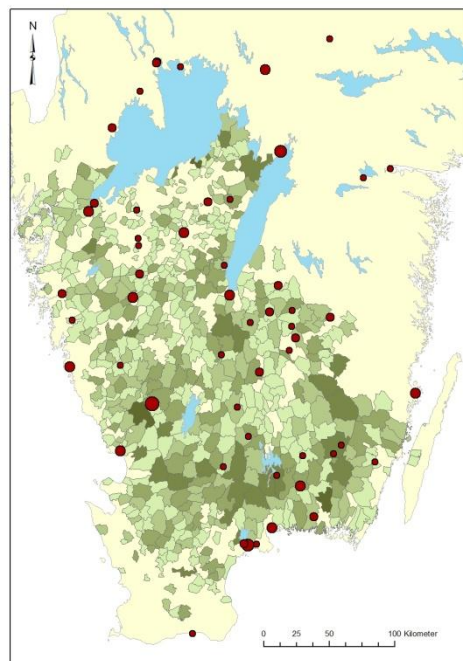
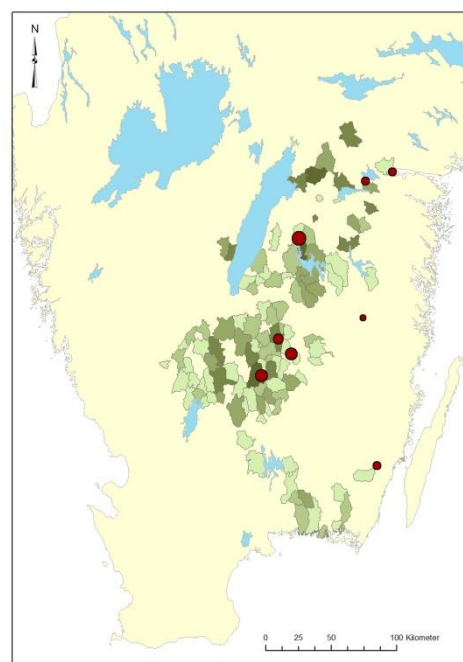
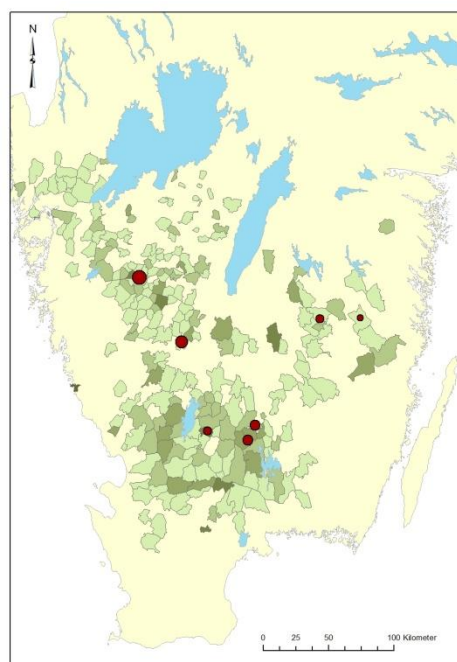
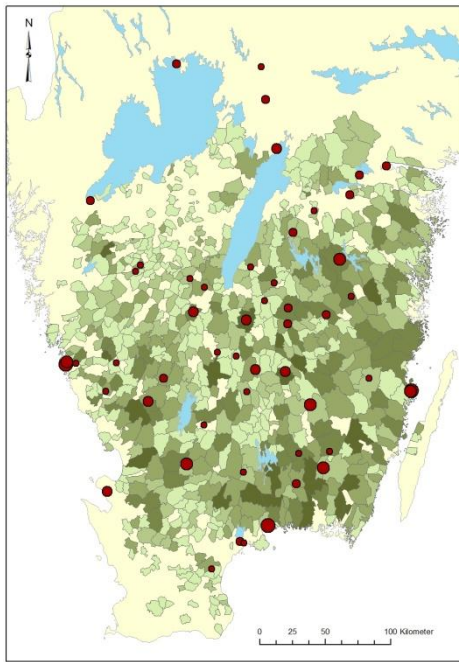
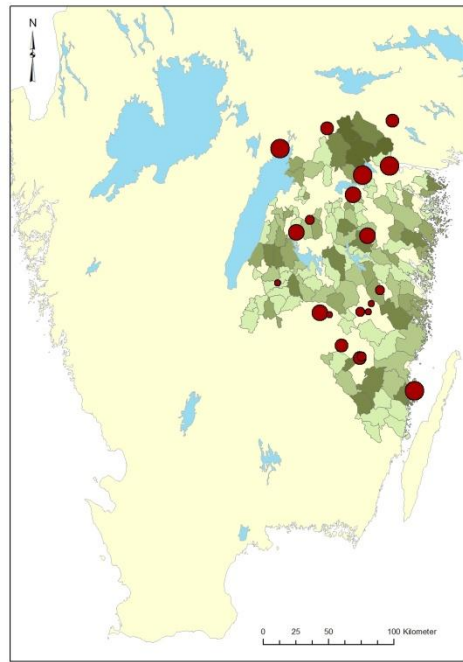


# Linear Production Game

- In fact: A Hitchcock-Koopmans transportation Game

# Cost allocation based on volume

Company	Individual	Volume	%
Company 1	3,778	3,439	<b>9,0</b>
Company 2	14,859	13,411	<b>9,7</b>
Company 3	4,742	4,213	<b>11,2</b>
Company 4	2,067	1,979	<b>4,3</b>
Company 5	10,340	10,318	<b>0,2</b>
Company 6	4,959	3,971	<b>19,9</b>
Company 7	1,884	1,635	<b>13,2</b>
Company 8	0,333	0,287	<b>14,0</b>
<b>Sum</b>	<b>42,963</b>	<b>39,253</b>	



# Game theory approach – Basics

coalition  $S$  : a subset of participants  $N$  (or players)

grand coalition  $S = N$  : all participants

$c(S)$ : cost for the transportation for  $S$

Efficient allocation :  $\sum_{j \in N} y_j = c(N)$

Individual rationality :  $y_j \leq c(\{j\})$

Core :  $\sum_{j \in S} y_j \leq c(S), \quad S \subset N$

$\sum_{j \in N} y_j = c(N)$  (efficiency)

# Models

Volume based allocation :  $y_j = w_j c(N)$

$w_j$  is equal to participant  $j$ 's share of the total volume

Shapley value :  $y_j = \sum_{S \subset N: j \in S} \frac{(|S|-1)!(|N|-|S|)!}{|N|!} [c(S) - c(S - j)]$

The Nucleolus : minimize the maximum dissatisfaction

If the core is non - empty, the nucleolus is in the core, i.e. it is stable.

Shadow prices :  $c(N) = \sum_{i \in I} u_i s_i + \sum_{k \in K} v_k d_k$

shadow prices :  $u_i, v_k$       supply, demand :  $s_i, d_k$

# Volume vs Shapley value

Company	Volume	%	Shapley	%
Company 1	3,439	<b>9,0</b>	3,586	<b>5,1</b>
Company 2	13,411	<b>9,7</b>	13,528	<b>9,0</b>
Company 3	4,213	<b>11,2</b>	4,102	<b>13,5</b>
Company 4	1,979	<b>4,3</b>	1,889	<b>8,6</b>
Company 5	10,318	<b>0,2</b>	9,747	<b>5,7</b>
Company 6	3,971	<b>19,9</b>	4,503	<b>9,2</b>
Company 7	1,635	<b>13,2</b>	1,587	<b>15,8</b>
Company 8	0,287	<b>14,0</b>	0,310	<b>6,9</b>
<b>Sum</b>	<b>39,253</b>		<b>39,253</b>	
Stable	No		Yes	

# Nucleolus

Company	Volume	Shapley	Shadow	Nucleolus
Company 1	9,0	5,1	4,1	<b>3,4</b>
Company 2	9,7	9,0	12,7	<b>11,1</b>
Company 3	11,2	13,5	14,2	<b>14,0</b>
Company 4	4,3	8,6	13,3	<b>6,4</b>
Company 5	0,2	5,7	-1,8	<b>4,8</b>
Company 6	19,9	9,2	11,7	<b>8,3</b>
Company 7	13,2	15,8	15,6	<b>11,5</b>
Company 8	14,0	6,9	9,1	<b>4,6</b>

# Model – Equal Profit Method

Relative saving:  $\frac{c(K) - y_i}{c(K)} = 1 - \frac{y_i}{c(K)}$  Stable allocation  $c(K) \geq y_i$ .

Relative difference between two participants:  $\frac{y_i}{c(K)} - \frac{y_j}{c(K)}$

Minimize difference i.e.

$$\min f$$

$$\text{s.t. } f \geq \frac{y_i}{c(K)} - \frac{y_j}{c(K)}$$

$$\sum_{j \in S} y_j \leq c(S), \quad S \subset N$$

$$\sum_{j \in N} y_j = c(N)$$



# EPM

Company	Volume	Shapley	Shadow	Nucleo.	EPM
Company 1	9,0	5,1	4,1	3,4	<b>6,7</b>
Company 2	9,7	9,0	12,7	11,1	<b>8,8</b>
Company 3	11,2	13,5	14,2	14,0	<b>8,8</b>
Company 4	4,3	8,6	13,3	6,4	<b>8,8</b>
Company 5	0,2	5,7	-1,8	4,8	<b>8,8</b>
Company 6	19,9	9,2	11,7	8,3	<b>8,8</b>
Company 7	13,2	15,8	15,6	11,5	<b>8,8</b>
Company 8	14,0	6,9	9,1	4,6	<b>8,8</b>

# Coalition Formation

- Insinking: A Methodology to Synergy in Transportation

Cruijssen, Borm and Fleuren Tilburg University

Does there exist a monotone Shapley path?

Answer: Depends on the sequence

Monotonic Paths,  
Rational Monotonic Paths,  
Monotonic Incomplete Paths

Combinations	.AR	.RR	.AN	.RN
S..	-	<b>18</b>	<b>18</b>	<b>18</b>
E..	-	<b>2428</b>	<b>2428</b>	<b>2428</b>
N..	-	170	133	170

# Savings Requirement when adding a new player to the sequence

$$\frac{(y_j^p - y_j)}{c(\{j\})} \geq \delta \quad , j \in \{j_1, j_2, \dots, j_p\}, \quad (**)$$

# No. of paths as a function of delta

$\delta$	$5.0 \cdot 10^{-4}$	$7.0 \cdot 10^{-4}$	$9.0 \cdot 10^{-4}$	$9.5 \cdot 10^{-4}$	$9.7 \cdot 10^{-4}$	$9.714611 \cdot 10^{-4}$	$9.714612 \cdot 10^{-4}$
No of MPs	900	256	10	4	3	3	0

# The three last remaining sequences

- (8,6,2,7,4,1,5,3)
- (8,2,7,6,4,1,5,3)
- (8,2,6,7,4,1,5,3)

# Filtering process

- Phase 1:
  - Solve full collaboration
  - Solve problem for each individual company
  - Remove all flows that are the same, fixed part
  - Remaining data, filtered part
- Phase 2
  - Solve full collaboration for filtered part
  - Add fixed cost to cost allocation go get final allocation

# Filtering and EPM

Comp	Ind	Fixed	Filt	EPM	E+fix	%	tot
1	3,778	2,472	1,305	1,074	3,546	<b>17,8</b>	<b>6,1</b>
2	14,859	7,072	7,788	6,405	13,477	<b>17,8</b>	<b>9,3</b>
3	4,742	2,217	2,526	2,077	4,294	<b>17,8</b>	<b>9,5</b>
4	2,067	0,824	1,243	1,022	1,846	<b>17,8</b>	<b>10,7</b>
5	10,340	6,508	3,832	3,152	9,659	<b>17,8</b>	<b>6,6</b>
6	4,959	2,290	2,670	2,196	4,485	<b>17,8</b>	<b>9,6</b>
7	1,884	0,452	1,432	1,178	1,630	<b>17,8</b>	<b>13,5</b>
8	0,333	0,233	0,100	0,082	0,315	<b>17,8</b>	<b>5,3</b>
Sum	42,963	22,067	20,895	39,253			



# Practical results

- The overall potential savings are 15%.
- Co-ordination savings are about 8%.
- Average transportation distance is decreased by 18%.
- Transportation work can be reduced with 18%.
- Energy consumption can be reduced by 18% resulting in 950 tons of less CO<sub>2</sub>.
- Five companies are making plans for coordination

# Strategic Implications from Filtering

- What should each company report as their input to the cooperation?
- Fernandez, Fiestras-Janeiro, Garcia-Jurado, Puerto: Competition and Coordination in Non-Centralised Linear Production Games *Annals of Operation Research* 2005
- Does a Nash Equilibrium exist when players report strategically?

