# Dynamics of Power\*

Based on tutorial & panel lectures at Energy Systems Week, Cambridge UK

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\*Dynamik i Makten (i grossistledet elmarknaderna)

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May 19, 2011

# Outline

### 1 Can You Spot the Competitive Equilibrium?

- 2 Competitive Equilibria in Dynamic Markets
- 3 Coping with Uncertainty and Constraints

### 4 Conclusions





# Spot the Competitive Equilibrium

# Competitive Equilibrium

Standard economic setting

#### Perfect competition

Long-run setting with uncertainty:

$$\begin{split} K_{\rm D}(G_{\rm D}) &= \mathsf{E}\Big[\int e^{-\gamma t} \mathcal{W}_{\rm D}(t) \, dt\Big] \\ K_{\rm S}(G_{\rm S}) &= \mathsf{E}\Big[\int e^{-\gamma t} \mathcal{W}_{\rm S}(t), dt\Big] \end{split}$$

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#### Price-taking assumption

Key assumption of equilibrium theory: The price of power P(t) does not depend on the decisions of the market agents.

# Competitive Equilibrium Efficiency

#### Efficient Equilibrium

Social Planner's Problem:

$$\max \quad K(G) = \mathsf{E} \Big[ \int e^{-\gamma t} \big( \mathcal{W}_{\mathsf{S}}(t) + \mathcal{W}_{\mathsf{D}}(t) \big) \, dt \Big]$$

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- Suppose that there exists a price process  $\{P^*(t)\}$  that forms an equilibrium: The consumers and suppliers agree,  $G_{\rm S} = G_{\rm D} = G$ .
- Suppose the agreed upon decisions G solve the SPP.

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### Let's look for examples of efficient equilibria!

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Not efficient?

#### Australia, January 16, 2007



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Fires cause chaos – *Is this efficient?* 

#### Midwest ISO today: Friday afternoon, March 4, 2011

3:30 p.m.



Midwest ISO today: Friday afternoon, March 4, 2011

3:50 p.m.



#### Midwest ISO today: Friday afternoon, March 4, 2011

4:15 p.m.



#### Midwest ISO today: Friday afternoon, March 4, 2011

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Texas today: Winter of 2011



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There will be multiple autopsies of the causes for the latest power breakdowns ... Who profited off this near-meltdown and what can be done to incentivize power producers to maintain adequate reserve capacity for emergencies rather than waiting for emergency windfalls? – HOUSTON CHRONICLE, Feb 12, 2011

New report hits ERCOT, electricity deregulation: A report released Monday concludes that electric deregulation has cost Texas residential consumers more than \$11 billion in higher rates... – Dallas Morning News, Feb 14, 2011

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...forward markets do not mitigate market power... ...forward markets systematically enhance market power in some symmetric capacity-constrained markets..."

-Frederic Murphy and Yves Smeers, 2010

#### A typical day in the New Zealand power market on the N. Island



\$25 million dollars extracted by the generators in just six hours



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**Efficient?** Energy consultant Bryan Leyland said the high wholesale prices showed *how dysfunctional the electricity market is.* 

Jacking the prices up sends no worthwhile signal to anyone — it is nothing to do with a shortage of generating capacity, he said. It just exposes the nonsense of it all.

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**Efficient!** Preliminary view of NZ Electrical Authority: *Genesis was not guilty* of "manipulative", ... or "deceptive" conduct. However, high prices threatened to undermine confidence in, and ... damage the integrity and reputation of the wholesale electricity market 3:59 PM Friday May 6, 2011 www.nzherald.co.nz

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#### It's not just about power!

#### Retail prices of onions in India

Indian Rupee per kg



Source: Ministry of Consumer Affairs

India's ban on onion exports to Nepal ... caused wholesale price to jump 50% in a week. NepaliEconomy.com, Jan 3, 2011



Soaring onion prices pushed food inflation again to a double-digit mark... - Indian Express, Feb 12, 2011

In India, onion prices are as politically sensitive as mortgage rates are in Australia. ... rising cost of the staple has helped change governments in India. – Fidelity International, Jan 2011



# **Competitive Equilibria in Dynamic Markets**

# Electricity Markets Today

Two coupled markets

#### Day-ahead market (DAM):

Cleared one day prior to the production and delivery of energy: The ISO generates a schedule of generators to supply specific levels of power for each hour over the next 24 hour period.

Facilitates the scheduling of generating units, and allows for hedging against uncertainty

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#### Real-time market (RTM):

As supply and demand are not perfectly predictable, the RTM plays the role of fine-tuning this resource allocation process

#### RTM is the focus here

# RTM Model

Dynamic model for reserves

Cho & Meyn model: Math model explains volatile prices in power markets. SIAM News, Robinson. 2005.

- R(t) = Available power Demand = G(t) D(t)
- D(t) = Actual demand Forecast

For computation: Deviation in demand D is modeled as Brownian motion

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#### Economic Friction

Generation cannot increase instantaneously:

For all 
$$t\geq 0$$
 and  $t'>t$ ,  $\quad \displaystyle rac{G(t')-G(t)}{t'-t}\leq \zeta$ 

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In recent work we also impose lower bounds on generation, as well as network constraints.

## Market Analysis: *A beautiful world...* Perfect competition

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What does an efficient equilibrium look like?

Efficient Equilibrium

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Special case: Welfare functions are piecewise linear,

$$\begin{aligned} \mathcal{W}_{\mathrm{S}}(t) &:= P(t)G_{\mathrm{S}}(t) - cG_{\mathrm{S}}(t) \\ \mathcal{W}_{\mathrm{D}}(t) &:= v\min(D(t), G_{\mathrm{D}}(t)) \\ &- c^{\mathrm{bo}}\max(0, -R_{\mathrm{D}}(t)) - P(t)G_{\mathrm{D}}(t) \end{aligned}$$

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#### Key component of equilibrium theory: Perfect competition

#### Price-taking assumption:

The price of power P(t) in the RTM is assumed to be exogenous (it does not depend on the decisions of the market agents).

Second Welfare Theorem  $\Longleftrightarrow$  Lagrangian Decomposition

$$\max K(G) = \max_{G_{\rm S}} \mathsf{E} \Big[ \int e^{-\gamma t} \big( \mathcal{W}_{\rm S}(t) + \lambda(t) G_{\rm S}(t) \big) \, dt \Big] \\ + \max_{G_{\rm D}} \mathsf{E} \Big[ \int e^{-\gamma t} \big( \mathcal{W}_{\rm D}(t) - \lambda(t) G_{\rm D}(t) \big) \, dt \Big]$$

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For linear cost/utility, marginal value is piecewise constant,

$$p^*(r^e) = (v + c^{\text{bo}})\mathbb{I}\{r^e < 0\}$$

# Market Equilibrium

#### Price dynamics



 $P^*(t) = p^*(R^e(t))$ : The marginal value of power to the consumer

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 $P^*(t) = p^*(R^e(t))$ : The marginal value of power to the consumer Smoother prices obtained when cost/utility are strictly convex

### Familiar, right?

#### Real-world price dynamics



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$$v + c^{\rm bo} =$$
 \$100,000/MWh!





500



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However,



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**Theorem 2:** In this equilibrium, the average price is precisely the *marginal cost c*. **Proof:** Lagrangian relaxation of initial condition.

Illinois: July 1998

California: July 2000

is usually \$30





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**Theorem 2:** In this equilibrium, the average price is precisely the *marginal cost c*. **Proof:** Lagrangian relaxation of initial condition. *Is this a sustainable business?* 



### **Coping with Uncertainty and Constraints**

### Network Constraints

Entropic prices

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See [Wang et. al., 2011]

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See [Wang et. al., 2011]

#### Without price-caps, Australia might look like an efficient equilibrium:



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#### Requires consideration of coupled RTM and DAM. In summary:

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 $\Rightarrow$  Social welfare falls with wind.

[Value of Volatile Resources, CDC, 2010]

Distribution of welfare (consumers command wind resources)

#### With increased volatility: Consumer welfare falls, supplier welfare rises:



Penetration k, coefficient of variation  $c_v$ .

#### Conclusions



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Distributed control and prices

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How could two smart people come to such different conclusions? I had to get to the bottom of this. -MacKay 2009
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Planning and Policy, includes Markets & Competition Evolution? Too slow! What we need is Intelligent Design

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**Approach:** Follow the example of highway engineering

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**Approach:** Follow the example of highway engineering

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The economic security of the region is at stake: We need well-designed lanes and speed limits in the energy highway!

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The best architecture for tomorrow's energy highway? This is *the* central open question.

Its solution opens many exciting research challenges!

### Thanks!



Celebrating with Dutch Babies after finishing part of this work

References



#### Control Techniques FOR Complex Networks



Sean Meyn

CAMBRIDGE UNIVERSITY PRESS Markov Chains and Stochastic Stability



S. P. Meyn and R. L. Tweedie

CAMBRIDGE UNIVERSITY PRESS

#### References

#### References

#### References

- G. Wang, M. Negrete-Pincetic, A. Kowli, E. Shafieepoorfard, S. Meyn, and U. Shanbhag. Dynamic competitive equilibria in electricity markets. In A. Chakrabortty and M. Illic, editors, *Control and Optimization Theory for Electric Smart Grids*. Springer, 2011.
- M. Negrete-Pincetic and S. Meyn. Intelligence by design for the entropic grid. In *IEEE PES* 11: Power Energy Society General Meeting, 2011.

G. Wang, A. Kowli, M. Negrete-Pincetic, E. Shafieepoorfard, and S. Meyn. A control theorist's perspective on dynamic competitive equilibria in electricity markets. In *Proc. 18th World Congress of the International Federation of Automatic Control (IFAC)*, Milano, Italy, 2011.



S. Meyn, M. Negrete-Pincetic, G. Wang, A. Kowli, and E. Shafieepoorfard. The value of volatile resources in electricity markets. In *Proc. of the 10th IEEE Conf. on Dec. and Control*, Atlanta, GA, 2010.



I.-K. Cho and S. P. Meyn. Efficiency and marginal cost pricing in dynamic competitive markets with friction. *Theoretical Economics*, 5(2):215–239, 2010.

M. Chen, I.-K. Cho, and S. Meyn. Reliability by design in a distributed power transmission network. *Automatica*, 42:1267–1281, August 2006.